

Espressioni con frazioni di frazioni. Livello base. Completi di soluzione guidata.  
Evaluating Expressions Involving Complex Fractions – With solutions

1. 
$$\frac{1 - \frac{1}{3}}{1 - \frac{1}{2}}$$
 [soluzione](#)
2. 
$$\frac{\frac{1}{5}}{1 - \frac{1}{2} + \frac{1}{5}}$$
 [soluzione](#)
3. 
$$\frac{2 + \frac{2}{3}}{1 - \frac{1}{2}}$$
 
$$\left[ \frac{16}{3} \right]$$
 [soluzione](#)
4. 
$$\frac{1 - \frac{1}{3}}{1 + \frac{1}{3}}$$
 
$$\left[ \frac{1}{2} \right]$$
 [soluzione](#)
5. 
$$\frac{2 - \frac{1}{4}}{2 + \frac{1}{4}}$$
 
$$\left[ \frac{7}{9} \right]$$
 [soluzione](#)
6. 
$$\frac{\left(1 - \frac{5}{9}\right) : \left(1 - \frac{3}{5}\right)}{\left(2 + \frac{1}{3}\right) - \left(1 + \frac{1}{2}\right)}$$
 
$$\left[ \frac{4}{3} \right]$$
 [soluzione](#)
7. 
$$\frac{\left(\frac{7}{2} - 3\right) \cdot 2}{\left(1 + \frac{5}{8}\right) : \frac{13}{2}}$$
 
$$[4]$$
 [soluzione](#)
8. 
$$\frac{\frac{1}{4} + \frac{2}{3} - \frac{5}{4}}{1 - \frac{1}{3}}$$
 
$$\left[ \frac{1}{8} \right]$$
 [soluzione](#)
9. 
$$\frac{\left(\frac{7}{2} + \frac{1}{3}\right) : \left(7 + \frac{2}{3}\right)}{\left(1 + \frac{5}{4}\right) : 5}$$
 
$$\left[ \frac{10}{9} \right]$$
 [soluzione](#)

$$10. \frac{\frac{6}{5} - \frac{10}{9}}{\left(\frac{5}{4} + \frac{1}{20}\right) \cdot \frac{1}{9}} \quad \left[\frac{2}{3}\right]$$

[soluzione](#)

$$11. \frac{\left(1 + \frac{1}{3}\right) \cdot \left(1 - \frac{1}{2}\right) : \left(1 - \frac{1}{2}\right)}{\left(\frac{3}{2} - 1\right) \cdot 2 + \frac{1}{4}} \quad \left[\frac{16}{15}\right]$$

[soluzione](#)

$$12. \frac{\left(\frac{2}{3} - \frac{1}{2}\right) : \frac{7}{3}}{\frac{5}{9} \cdot \left(1 - \frac{7}{10}\right)} \quad \left[\frac{3}{7}\right]$$

[soluzione](#)

$$13. \frac{\frac{7}{6} + \frac{5}{3} - \frac{1}{2}}{\left(\frac{11}{12} + \frac{1}{3}\right) - \frac{1}{4}} \quad \left[\frac{7}{3}\right]$$

[soluzione](#)

$$14. \frac{1 - \frac{13}{18} + \frac{7}{21}}{1 + \frac{1}{9} + \frac{16}{20}} \quad \left[\frac{2}{3}\right]$$

[soluzione](#)

$$15. \frac{1}{1 + \frac{1}{1 + \frac{1}{3}}} \quad \left[\frac{4}{7}\right]$$

[soluzione](#)

$$16. \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}} \quad \left[\frac{3}{5}\right]$$

[soluzione](#)

$$17. \frac{2 \cdot \left(\frac{1}{3} + 2\right)}{3} - \frac{3 \cdot \frac{1}{3} - 1}{2} \quad \text{soluzione}$$

$$18. \frac{\frac{4}{3}}{1 - \frac{2}{3 + \frac{1}{2 - \frac{1}{3}}}} \quad \text{soluzione}$$

$$19. \frac{1}{1 + \frac{1}{1 + \frac{1}{7}}} \quad \text{soluzione}$$

## Soluzioni

$$\frac{1 - \frac{1}{3}}{1 - \frac{1}{2}}$$

Risoluzione diretta	Passando per il quoziente
$= \frac{\frac{3-1}{3}}{\frac{2-1}{2}} =$ $= \frac{\frac{2}{3}}{\frac{1}{2}} =$ $= \frac{2}{3} : \frac{1}{2} =$ $= \frac{2}{3} \cdot \frac{2}{1} = \frac{4}{3}$	$\left(1 - \frac{1}{3}\right) : \left(1 - \frac{1}{2}\right) =$ $= \left(\frac{3-1}{3}\right) : \left(\frac{2-1}{2}\right) =$ $= \frac{2}{3} : \frac{1}{2} =$ $= \frac{2}{3} \cdot \frac{2}{1} = \frac{4}{3}$

$$\frac{\frac{1}{5}}{1 - \frac{1}{2} + \frac{1}{5}}$$

Risoluzione diretta	Passando per il quoziente
$= \frac{\frac{1}{5}}{\frac{10-5+2}{10}} =$ $= \frac{\frac{1}{5}}{\frac{7}{10}} =$ $= \frac{1}{5} : \frac{7}{10} =$ $= \frac{1}{5} \cdot \frac{10}{2} = \frac{2}{7}$	$\frac{1}{5} : \left(1 - \frac{1}{2} + \frac{1}{5}\right) =$ $= \frac{1}{5} : \frac{10-5+2}{10} =$ $= \frac{1}{5} : \frac{7}{10} =$ $= \frac{1}{5} \cdot \frac{10}{2} = \frac{2}{7}$

$$\begin{aligned} & \frac{2 + \frac{2}{3}}{1 - \frac{1}{2}} = \\ & = \frac{\frac{6+2}{3}}{\frac{2-1}{2}} = \\ & = \frac{\frac{8}{3}}{\frac{1}{2}} = \frac{8}{3} \cdot \frac{2}{1} = \frac{16}{3} \end{aligned}$$

$$\begin{aligned} & \frac{1 - \frac{1}{3}}{1 + \frac{1}{3}} = \\ & \frac{\frac{3-1}{3}}{\frac{3+1}{3}} = \\ & \frac{2}{3} = \frac{2}{3} \cdot \frac{3}{4} = \frac{1}{2} \end{aligned}$$

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$$\begin{aligned} & \frac{2 - \frac{1}{4}}{2 + \frac{1}{4}} = \\ & \frac{\frac{8-1}{4}}{\frac{8+1}{4}} = \\ & \frac{7}{9} = \\ & \frac{7}{4} \cdot \frac{4}{9} = \frac{7}{9} \end{aligned}$$

$$\begin{aligned}
 & \frac{\left(1 - \frac{5}{9}\right) : \left(1 - \frac{3}{5}\right)}{\left(2 + \frac{1}{3}\right) - \left(1 + \frac{1}{2}\right)} = \\
 & = \frac{\left(\frac{9-5}{9}\right) : \left(\frac{5-3}{5}\right)}{\left(\frac{6+1}{3}\right) - \left(\frac{2+1}{2}\right)} = \\
 & = \frac{\frac{4}{9} \cdot \frac{5}{2}}{\frac{7}{3} - \frac{3}{2}} = \\
 & = \frac{\frac{10}{9}}{\frac{14-9}{6}} = \\
 & = \frac{\frac{10}{9}}{\frac{5}{6}} = \\
 & = \frac{10}{9} \cdot \frac{6}{5} = \frac{4}{3}
 \end{aligned}$$


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$$\begin{aligned}
 & \frac{\left(\frac{7}{2} - 3\right) \cdot 2}{\left(1 + \frac{5}{8}\right) : \frac{13}{2}} = \\
 & = \frac{\left(\frac{7-6}{2}\right) \cdot 2}{\left(\frac{8+5}{8}\right) \cdot \frac{2}{13}} = \\
 & = \frac{\left(\frac{1}{2}\right) \cdot 2}{\left(\frac{13}{8}\right) \cdot \frac{2}{13}} = \frac{1}{\frac{1}{4}} = 1 \cdot \frac{4}{1} = 4
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\frac{1}{4} + \frac{2}{3}}{1 - \frac{1}{3}} - \frac{5}{4} = \\
 & = \frac{3 + 8}{12} : \frac{3 - 1}{3} - \frac{5}{4} = \\
 & = \frac{11}{12} : \frac{2}{3} - \frac{5}{4} = \\
 & = \frac{11}{4} \cdot \frac{1}{2} - \frac{5}{4} = \\
 & = \frac{11}{8} - \frac{5}{4} = \\
 & = \frac{11 - 10}{8} = \frac{1}{8}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\left(\frac{7}{2} + \frac{1}{3}\right) : \left(7 + \frac{2}{3}\right)}{\left(1 + \frac{5}{4}\right) : 5} = \\
 & = \frac{\left(\frac{21+2}{6}\right) : \left(\frac{21+2}{3}\right)}{\left(\frac{4+5}{4}\right) \cdot \frac{1}{5}} = \\
 & = \frac{\frac{23}{6} \cdot \frac{3}{23}}{\left(\frac{9}{4}\right) \cdot \frac{1}{5}} = \\
 & = \frac{\frac{1}{2}}{\frac{9}{20}} = \frac{1}{2} \cdot \frac{20}{9} = \frac{10}{9}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\frac{6}{5} - \frac{10}{9}}{\left(\frac{5}{4} + \frac{1}{20}\right) \cdot \frac{1}{9}} = \\
 & \frac{\frac{54 - 50}{45}}{\left(\frac{25 - 1}{20}\right) \cdot \frac{1}{9}} = \\
 & \frac{\frac{4}{45}}{\left(\frac{24}{20}\right) \cdot \frac{1}{9}} = \\
 & \frac{\frac{4}{45}}{\left(\frac{6}{5}\right) \cdot \frac{1}{9}} = \left(\frac{4}{45} \cdot \frac{5}{6} \cdot \frac{9}{1}\right) = \frac{2}{3}
 \end{aligned}$$


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$$\begin{aligned}
 & \frac{\left(1 + \frac{1}{3}\right) \cdot \left(1 - \frac{1}{2}\right) : \left(1 - \frac{1}{2}\right)}{\left(\frac{3}{2} - 1\right) \cdot 2 + \frac{1}{4}} = \\
 & \frac{\left(\frac{4}{3}\right) \cdot \left(\frac{1}{2}\right) : \left(\frac{1}{2}\right)}{\frac{1}{2} \cdot 2 + \frac{1}{4}} = \\
 & \frac{\frac{4}{3}}{1 + \frac{1}{4}} = \frac{4}{3} \cdot \frac{4}{5} = \frac{16}{15}
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{2}{3} - \frac{1}{2} \right) \div \frac{7}{3} = \\
 & \frac{5}{9} \cdot \left( 1 - \frac{7}{10} \right) = \\
 & \left( \frac{4-3}{6} \right) \cdot \frac{3}{7} = \\
 & \frac{5}{9} \cdot \left( \frac{10-7}{10} \right) = \\
 & \left( \frac{1}{6} \right) \cdot \frac{3}{7} = \\
 & \frac{5}{9} \cdot \left( \frac{3}{10} \right) = \\
 & \frac{1}{6} = \frac{14}{1} = \left( \frac{1}{14} \cdot \frac{6}{1} \right) = \frac{3}{7}
 \end{aligned}$$


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$$\begin{aligned}
 & \frac{7}{6} + \frac{5}{3} - \frac{1}{2} = \\
 & \left( \frac{11}{12} + \frac{1}{3} \right) - \frac{1}{4} = \\
 & \frac{7+10-3}{6} = \\
 & \left( \frac{11+4}{12} \right) - \frac{1}{4} = \\
 & \frac{14}{12} - \frac{1}{4} = \\
 & \frac{14}{15} - \frac{1}{4} = \\
 & \frac{14}{15-3} = \\
 & \frac{14}{12} = \frac{7}{6} = \frac{7}{3}
 \end{aligned}$$

$$\begin{aligned}
 & 1 - \frac{13}{18} + \frac{7}{21} \\
 & \frac{18-13}{18} + \frac{16}{21} = \\
 & 1 + \frac{5}{9} + \frac{16}{21} = \\
 & \frac{18-13}{9} + \frac{7}{16} \cdot \frac{20}{21} = \\
 & \frac{5}{9} + \frac{1}{4} \cdot \frac{5}{3} = \\
 & \frac{5}{9} + \frac{5}{12} = \frac{4}{9} + \frac{5}{12} = \frac{16}{36} + \frac{15}{36} = \frac{31}{36}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{1 + \frac{1}{1 + \frac{1}{3}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{3+1}{3}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{4}{3}}} = \\
 & = \frac{1}{1 + 1 \cdot \frac{3}{4}} = \\
 & = \frac{1}{1 + \frac{3}{4}} = \\
 & = \frac{1}{\frac{4+3}{4}} = \frac{1}{\frac{7}{4}} = 1 \cdot \frac{4}{7} = \frac{4}{7}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{2+1}{2}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{3}{2}}} = \\
 & = \frac{1}{1 + 1 \cdot \frac{2}{3}} = \\
 & = \frac{1}{1 + 1 \cdot \frac{2}{3}} = \\
 & = \frac{1}{1 + \frac{2}{3}} = \\
 & = \frac{1}{\frac{3+2}{3}} = \\
 & = \frac{1}{\frac{5}{3}} = \\
 & = 1 \cdot \frac{3}{5} = 1 \cdot \frac{3}{5} = \frac{3}{5}
 \end{aligned}$$


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$$\begin{aligned}
 & \frac{2 \cdot \left(\frac{1}{3} + 2\right)}{3} - \frac{3 \cdot \frac{1}{3} - 1}{2} = \\
 & = \frac{2 \cdot \frac{7}{3}}{3} - \frac{1 - 1}{2} = \\
 & = \frac{2 \cdot \frac{7}{3}}{3} - \frac{1 - 1}{2} = \\
 & = \frac{14}{3} \cdot \frac{1}{3} = \frac{14}{9}
 \end{aligned}$$



$$\begin{aligned}
 & \frac{\frac{4}{3}}{1 - \frac{2}{3 + \frac{1}{2 - \frac{1}{3}}}} = \\
 & = \frac{\frac{4}{3}}{1 - \frac{2}{3 + \frac{1}{\frac{5}{3}}}} = \\
 & = \frac{\frac{4}{3}}{1 - \frac{2}{3 + \frac{3}{5}}} = \\
 & = \frac{\frac{4}{3}}{1 - \frac{2}{\frac{18}{5}}} = \\
 & = \frac{\frac{4}{3}}{1 - \frac{5}{9}} = \frac{\frac{4}{3}}{\frac{4}{9}} = \frac{4}{3} \cdot \frac{9}{4} = 3
 \end{aligned}$$



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$$\begin{aligned}
 & \frac{1}{1 + \frac{1}{1 + \frac{1}{7}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{7+1}{7}}} = \\
 & = \frac{1}{1 + \frac{1}{\frac{8}{7}}} = \\
 & = \frac{1}{1 + \frac{7}{8}} = \frac{1}{\frac{8+7}{8}} = \frac{1}{\frac{15}{8}} = \frac{8}{15}
 \end{aligned}$$


## Keywords

 *Matematica, Aritmetica, Frazioni, Espressioni Q, addizione, sottrazione, moltiplicazione, divisione, esercizi con soluzioni*

  *Math, Arithmetic, Fraction expressions, Fraction, Expression, Addition, Subtraction, Multiplication, Division, Fraction expressions solved*

 *Matemática, Aritmética, Fracción, Expresiones, Resta, Sustracción, Suma, Adición, Multiplicación, División*

 *Mathématique, Arithmétique, Fraction, Problèmes avec fractions, Addition, Soustraction, Multiplication, Division*

 *Mathematik, Arithmetik, Bruchrechnung, Bruch, Subtraktion, Addition, Multiplikation, Division*

Arabic: كَسْر

Chinese (Simplified): 分数

Chinese (Traditional): 分數

Czech: zlomek

Danish: brøkdæl

Dutch: deel, breuk

Estonian: murd(arv)

Finnish: murtoluku

French: fraction

Greek: κλάσμα

Hungarian: hányad, tört(rész)

Icelandic: brot

Indonesian: pecahan

Japanese: 分数

Korean: 분수

Lithuanian: trupmena

Norwegian: brøk(del)

Polish: ułamek

Portuguese (Brazil): fração

Portuguese (Portugal): fracção

Romanian: fracție

Russian: дробь

Slovak: zlomek

Slovenian: ulomek

Swedish: del

Turkish: kesir